

## es-hist-is-concat<sup>11,40</sup>

$\forall ds:\text{fpf}(\text{Id}; x.\text{Type}), da:\text{fpf}(\text{Knd}; k.\text{Type}), es:\text{event\_system}\{\text{i:l}\}, i:\text{Id},$   
 $LL:(\text{event-info}(ds;da) \text{ List List}), e_1,e_2:\{e:\text{es-E}(es) | \text{loc}(e) = i\},$   
 $L:(\text{event-info}(ds;da) \text{ List}).$   
 $\text{l_all}(LL; (\text{event-info}(ds;da) \text{ List}); L.(\neg(L = [])))$   
 $\Rightarrow (\neg(L = []))$   
 $\Rightarrow (\forall x:\text{Id}. \text{ subtype_rel(es-vartype}(es; i; x); \text{fpf-cap}(ds; id-deq; x; top)))$   
 $\Rightarrow (\forall e:\text{es-E}(es).$   
 $(\text{loc}(e) = i)$   
 $\Rightarrow \text{subtype_rel(es-valtype}(es; e); \text{fpf-cap}(da; \text{Kind-deq}; \text{es-kind}(es; e); \text{top}))$   
 $\Rightarrow (\text{es-hist}\{\text{i:l}\}(es;e_1;e_2) = \text{append(concat}(LL); L) \in (\text{event-info}(ds;da) \text{ List}))$   
 $\Rightarrow (\exists f:\text{int\_seg}(0; (\|LL\| + 1)) \rightarrow \{e:\text{es-E}(es) | \text{loc}(e) = i\}$   
 $((f(0) = e_1) \wedge \text{es-le}(es; (f(\|LL\|)); e_2))$   
 $\wedge (\forall i:\text{int\_seg}(0; \|LL\|). \text{es-locl}(es; (f(i)); (f(i + 1))))$   
 $\wedge ((\forall i:\text{int\_seg}(0; \|LL\|).$   
 $\text{es-hist}\{\text{i:l}\}(es;f(i);\text{es-pred}(es; (f(i + 1)))) = LL[i] \in (\text{event-info}(ds;da) \text{ List}))$   
 $\wedge (\text{es-hist}\{\text{i:l}\}(es;f(\|LL\|);e_2) = L)))$